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Symbols

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 $\in$ (set member), 49
 $\subseteq$ (subset), 49
 $\subset$ (proper subset), 49
 $\cap$ (set intersection), 49
 $\cup$ (set union), 49
 $-$ (set difference), 49
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 $\lceil \cdot \rceil$ (ceiling), 49
 ϕ (Euler phi function), 65, 286
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 $\ln$ (natural logarithm), 50
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 $\gg$ (much greater than), 170
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 $\left(\frac{a}{p}\right)$ (Legendre symbol), 72
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